

3rd Congress of Balkan Geophysical Society
Sofia 24-28 May, 2002. Bulgaria.

**DIPOLE – DIPOLE ARRAY CONFIGURATION IN THE FRAMEWORK OF THE
RECIPROCITY PRINCIPLE**

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Abstract

In the paper it is discussed the change of configuration of IP and resistivity anomalies for dipole-dipole and pole-dipole arrays. The analysis is done based on results of 2D and 3D mathematical modeling carried out successfully in the framework of scientific research of QUANTEC GEOSCIENCE Ltd., Toronto, Ontario, Canada, and of physical modeling done in the Geophysical Laboratory "Ligor Lubonja" of the Faculty of Geology and Mining, Polytechnic University of Tirana.

Key words: dipole-dipole survey configuration, Reciprocity Principle, IP anomaly, Apparent resistivity anomaly.

Introduction

In the practice of electrical prospecting are employed various array configurations. The location of the current and potential electrodes is defined from the geological tasks to be solved. The Dipole – Dipole array is one of the most common arrays in mineral exploration. This is considered a symmetrical array in terms of the principle of reciprocity, so when the current electrodes are respectively switched with potential electrodes the same responses in IP and resistivity values are observed. However, our recent mathematical models indicate some distortions of the reciprocity principle in IP/Resistivity responses with a Dipole – Dipole array. This can lead to inaccurate target location and negative drilling results.

Presentation of Problem

The well-known reciprocity principle stands on the basis of many array configurations in electrical prospecting like Pole - Pole, Dipole - Dipole, Schlumberger, Wenner etc (Keller, G., V. and Frischknecht, F., C.,1970, Zabarovsky A. 1963, I., Fraseri, A., et al. 1985). “According to the theorem of the reciprocity, no changes will be observed in the measured voltage if the role of measuring electrodes and of the current electrodes are interchanges. Reciprocity can be readily confirmed for an electrode array over a homogeneous earth” (Keller, G., V. and Frischknecht, F., C.,1970).

There is another problem for heterogeneous mediums. Zabarovsky, A.I. (1963) shows that if a body A has received an electrical charge Q_A , a body M will have a potential U_M related with the charge Q_A following the equation:

$$U_M = \alpha_{AM} \cdot Q_A$$

where α_{AM} is a coefficient dependant on the shape of bodies A and M, their reciprocal position and the boundaries of heterogeneity. If the reversed operation would take place, i.e. the body M to receive electrical charges of Q_M then the potential U_A of the body A would be:

$$U_A = \alpha_{MA} \cdot Q_M$$

" In electrostatic phenomena science it is shown that $\alpha_{AM} = \alpha_{MA}$. If this equality is true, then $Q_M=Q_A$ and as consequence $U_M=U_A$. Translating this result in the language of electrodynamics, one may say that the potential of electrode M created by the effect of the electrode A would be equal to the potential of the electrode A, if the currents would be emitted in ground by the electrode M, with the condition that the product $I * \rho$ remains the same". On this basis he concluded that the principle of reciprocity is valid for heterogeneous mediums as well.

This conclusion is true for some arrays used for electrical surveys of apparent resistivity methods. Four electrodes Schlumberger array AMNB is reciprocal with the array MABN, pole-pole array C_1P_1 is reciprocal with P_1C_1 . The pole-dipole array $P_1P_2C_1$ is reciprocal with $C_1C_2P_1$ (Fraseri, A. et al. 1985). But these reciprocities of current and receiving electrodes are not equivalent with the change of positions of couples of electrodes during profiling, in the relation to the heterogeneity. The pole-dipole array $C_1P_2P_1$ is not reciprocal with the $P_1P_2C_1$. The pole-dipole array is known as an asymmetric array. The same is for the dipole-dipole array $C_1C_2P_1P_2$ relative to $P_1P_2C_1C_2$. All this is connected with the well-known fact that pole-dipole and dipole-dipole arrays give asymmetrical anomalies for the apparent resistivity.

These changes are more evident in IP surveys. In several field surveys some asymmetrical responses are observed with a Dipole – Dipole array ($C_1C_2P_1P_2$ versus $P_1P_2C_1C_2$) in both IP and resistivity measurements. To further investigate this phenomenon some mathematical models were carried out with a program of finite element method (Fraseri A. and Fraseri N. 2000).

This analysis was initiated because of the fact that, in daily practices of geoelectrical surveys using dipole-dipole profiling a little attention is shown towards the evaluation of anomaly configuration depending on the position of couples of current and receiving electrodes. In many publications with the results of modeling and of inversion, the position of electrodes on surveying line is not shown (Dey, A., and Morrison, H. F., 1979, Tsourlos, P.I., et al., 1998, Tsourlos, P. I. and Ogilvy, R. D. 1999). This has consequences in the results of interpretation relative to spatial position of exciting bodies.

Mathematical modeling of the IP effect have based on the Bleil formulae [Bleil D., 1953; Seigel H.O., 1959]:

$$U_{IP} = c \cdot \int_V \nabla U \cdot \left(\frac{1}{R} \right) \cdot dv \quad (1)$$

Where: U_{ip} is the IP potential;

\vec{R} is the distance vector from the integration point to the receiving point;

∇U is the potential gradient of the primary electrical field, calculated by solving the finite element model.

To achieve the mathematical modeling and the inversion of IP data, we have used the evaluation of Komarov V.A., which is expressed with the formulae [Komarov V.A., 1972]:

$$C(U_0 + U_{ip}) \approx CU_0 \quad (2)$$

where: U_0 is the potential of the field of primary electrical currents,
 U_{ip} is the potential of the field of induced polarization,
 C is the IP susceptibility.

Based on mathematical modeling of IP anomalous field, there is a formal similarity of the polarizable medium and the increasing of electrical specific resistivity of this medium as proposed by [Komarov V.A., 1972] and used by many other authors (Avdeevic M.M., Fokin A.F., Frasher A. 1989, Frasher et al 1994, Frasher A., Frasher N. 2000, Hmelevskoj V.K., Shevshin V.A. 1994, Tsourlos P.I., Szymanski J.E., Tsokas G.N., 1998, Tsourlos P.I., Ogilvy R.D., 1999):

$$\gamma^* = \gamma(1-m) \quad \text{or} \quad \rho^* = \frac{1}{\gamma(1-m)}; \quad (3)$$

where: γ^* , ρ^* are fictive electrical conductivity and resistivity, considering the polarizability as well,
 γ is electrical conductivity
 m is IP chargeability

Consequently, induced polarization is considered as linear phenomenon.

For 3D modeling of IP effect from targets with massive texture in homogeneous medium we have transformed the Bleil formulae, using Green's formulae (Frasher N. 1983, Frasher A., Frasher N. 2000):

$$U_{IP} = c \cdot \int_S \left(\frac{1}{R} \right) \cdot \left(\frac{dU}{dn} \right) \cdot ds \quad (4)$$

Where: R is the distance vector from the integration point to the measurement point;
 dU/dn is the gradient of the primary electrical potential on the boundary S of the target.

Ne figuren 1 tregohet rezultati i nje modelimi matematik te PP, te realizuar me anen e metodes se elementeve te fundme, i krahasuar me anomaline e vrojtuar ne terren.

With the same method of finite elements, simultaneously with the IP effect, the apparent resistivity is calculated as well.

Ne fig. 2 jepet krahasimi i anomalise se llagaritur me programin e mesipermdhe asaj teorike si edhe anomalise se vrojtuar ne modelime fizike. Nga te dy ket raste konstatohet se saktesia e modelimit matematik eshte e mire.

Konceptimi i IP si fenomen linear, ka sjelle qw ne modelimet matematike, IP anomalite e kalkuluara te ndryshojne nga ato te rezistences (fig. 3) Ne keto sections konstatohet se:

- Skaji i siperm i anomalive perputhet mire me skajin e sipert te target e polarizueshem,
- IP Anomaly mbetet e hapur drejt thellesise edhe nen skajin e poshtem te target. Ne ndryshim nga kjo, anomalia e rezistences se dukshme mbyllet nen nivelin e trupit. Te njejtin fenomen ka verejtur edhe Komarov V.A. (1972) ne IP Vertical Sounding.

Numerical results for different models

Figs. 4 and 5 present the mathematical model results of IP and resistivity responses with dipole-dipole profiling. Two anomalies are observed in both parameters. Considering the reference plotting point in between the potential electrodes P_1 and P_2 , one of the anomalies is obtained over the prism while the second one at a distance O_1O_2 , between the centers of the current and potential dipoles. This presentation is conditioned on the distribution of the electrical field of the dipole - dipole array. Because a mirror image is missing in the center of the profiles, especially for IP, it means that $C_1C_2P_1P_2$ array responses are not equivalent with $P_1P_2C_1C_2$, or in mathematical terms, the principle of reciprocity is not strictly met. Keller, G., V. (1970) also presents the same phenomenon for the apparent resistivity.

In pseudosection presentation, where the plotting point is located at the intersection of lines coming at 45° from midpoints between C_1C_2 and P_1P_2 , these anomalies are located in both sides of the prism (Figs. 6, 7, 8, 9). For the resistivity parameter this location is almost symmetrical in shape and amplitude, for the vertical target (Fig. 6). The symmetry is perfect in cases when the thickness of the prism is equal or greater than the dipole spacing "a", and becomes poor for thinner prisms (Fig. 9).

Alternatively, the IP anomalies are asymmetrical even in cases of vertical prisms (Fig. 6 and 9). In such cases, the epicenter of the most intensive anomaly is displaced on the side of current dipole C_1C_2 . For shallow inclined prisms, the epicenters of both IP and resistivity anomalies are displaced on the opposite side of the dip. In cases of deep inclined prisms, the displacement is in the dip direction, providing that this is in the direction of the current electrodes (Fig.3).

The configuration of the IP/Resistivity anomaly is also dependent on the dip angle amplitude, relative to the current electrodes location.

The amplitude and the asymmetry of IP anomaly depend on the orientation of the polarizing vector of the primary field in connection with the prism location. In fig. 10 is presented the electric polarizing field distribution for the gradient array and dipole-dipole array. The great difference between distribution of the electric field in both cases, very well express the changes of the IP anomaly configuration for gradient and dipole-dipole array. In Fig. 11 is presented the changes of the anomaly configuration in the dependence of the location of the target, in relation with the current electrodes.

The same configuration of IP and resistivity anomalies is observed by physical modeling.

Anomalous tableau becomes more complicated when several exciting bodies are located under the surveying line. It is sufficient that the distance between two bodies to be less than 0.5 of their extension in depth, that over these bodies a single anomaly is received, being too wide and with the epicenter over the space between bodies (Fig. 12, 13). Such situation does not permit a correct interpretation of the anomaly during the inversion process. In opposite, in the real section with multiple gradient array, two separate anomalies are observed (Fig. 14).

Asymmetrical IP and resistivity anomalies, in dependence of the location of current and potential dipoles in relation with the target, shows that the lack of orientation in the current and potential electrodes is not always without problems in manual or inversion interpretations of the IP/Resistivity data surveyed with a dipole–dipole array.

Conclusions

1. The anomaly configuration in an IP/Resistivity survey with a dipole–dipole array is dependent on the location of the current and potential electrodes in connection to target. In this regard, logistical information about the survey should include the array orientation (left-array or right-array). The position of the array must be shown in plots and pseudosections. During the profiling, it is necessary to keep the same configuration of current and receiving dipoles.
2. The results of the survey should be interpreted accordingly the array orientation in the survey line, in order to define the placement of exciting bodies, the direction of its inclination and the its depth. The same recommendation is valid for the process of inversion.
3. Profiling with dipole-dipole arrays has smaller discriminative capability for IP surveys, compared with other arrays as the gradient array.

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LIST OF CAPTIONS

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Fig. 2. IP profiling over a prism: Theoretical, calculated and physical modeling.

Fig. 3. IP and Ro Realsections with multiple gradient arrays. Mathematical model.

Model: horizontal prism at depth $2 D_x$, dimensions of the prism $1 \times 1 \times 20 D_x$. Prism Resistivity $2\ 000\ \text{Ohmm}$, IP Chargeability $100\ \text{mV/V}$, Environment Resistivity $1\ 000\ \text{Ohmm}$, IP Chargeability $1\ \text{mV/V}$.

Fig. 4. IP and Resistivity mathematical modeling. Dipole-dipole profiling, $C_1C_2-P_1P_2=1 D_x$, $n=16 D_x$.

Model: 2D horizontal prism at depth $5 D_x$, dimensions of the prism section $2 \times 2 D_x$. Resistivity of the prism $1\ \text{Ohmm}$, IP Chargeability $500\ \text{mV/V}$, Resistivity of the environment $1\ 000\ \text{Ohmm}$, IP Chargeability of the environment $0.01\ \text{mV/V}$.

- Fig. 5. IP and Resistivity mathematical modeling. Dipole-dipole profiling. $C_1C_2-P_1P_2=2$ Dx, $n=1-10$ Dx.
Model: 2D vertical prism at depth 1 Dx, dimensions of the prism section 2 x 9 Dx. Resistivity of the prism 20 000 Ohmm, IP Chargeability 500 mV/V, Resistivity of the environment 1 000 Ohmm, IP Chargeability of the environment 0.01 mV/V.
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- Fig. 7. IP and Resistivity Pseudosection with dipole-dipole array, $C_1C_2-P_1P_2=1$ Dx, $n=1-11$ Dx.
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- Fig. 11. Dependence of IP anomalies configuration from location of the target.
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IP contour interval 2 mV/V.
Mathematical Model: Two parallel inclined prisms (dip= 70°) at depth 5 Dx, dimensions of the prisms 1 x 20 x 20 Dx. Distance between the prisms 10 Dx, Prisms Resistivity 2 000 Ohmm, IP Chargeability 500 mV/V, Environment Resistivity 500 Ohmm, IP Chargeability 1 mV/V.
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F.E.M. MODELLING OF IP OF AN IRREGULAR BODY OVER RELIEFF

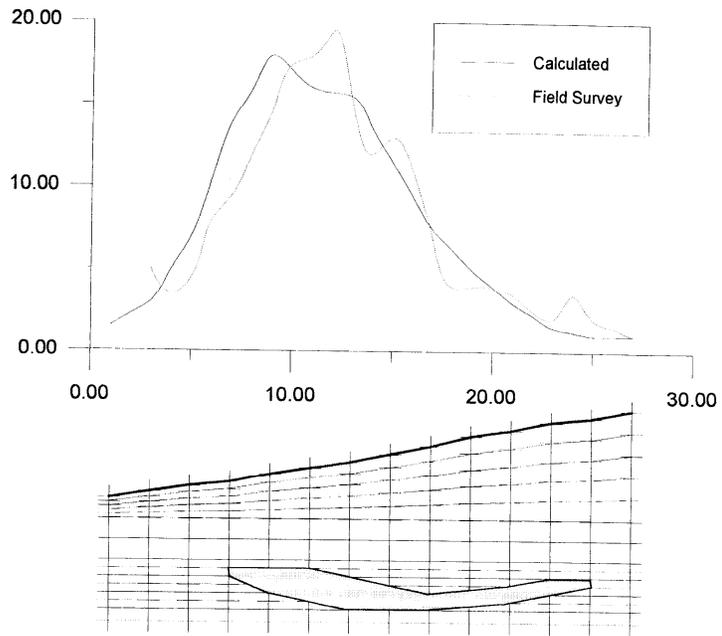


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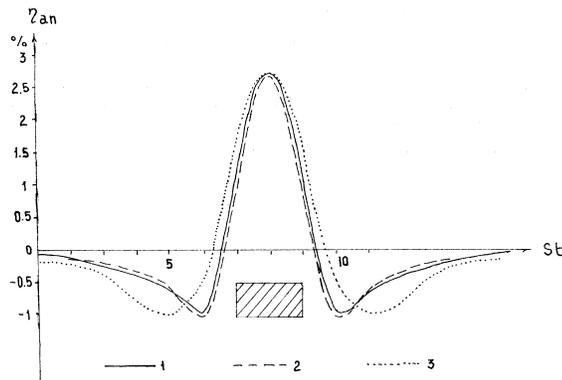


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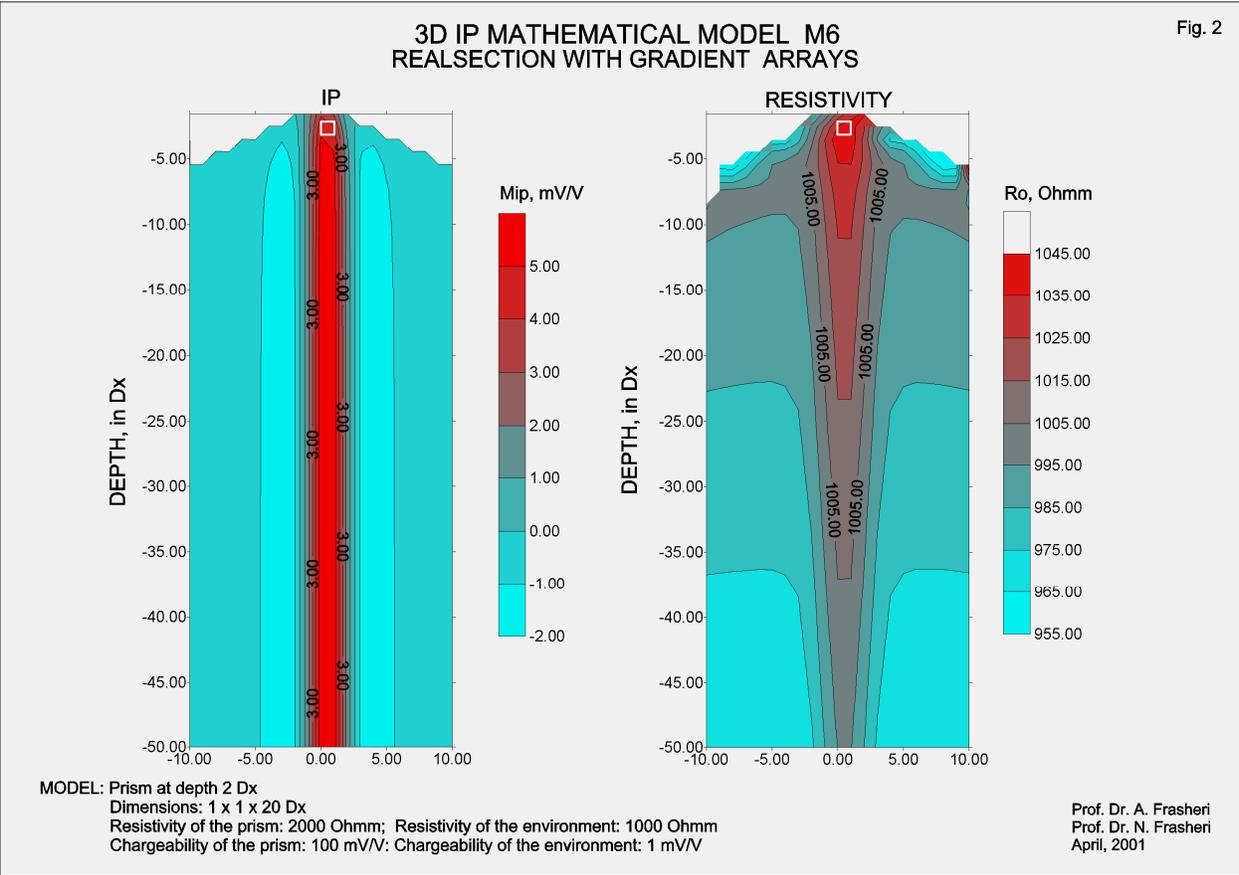


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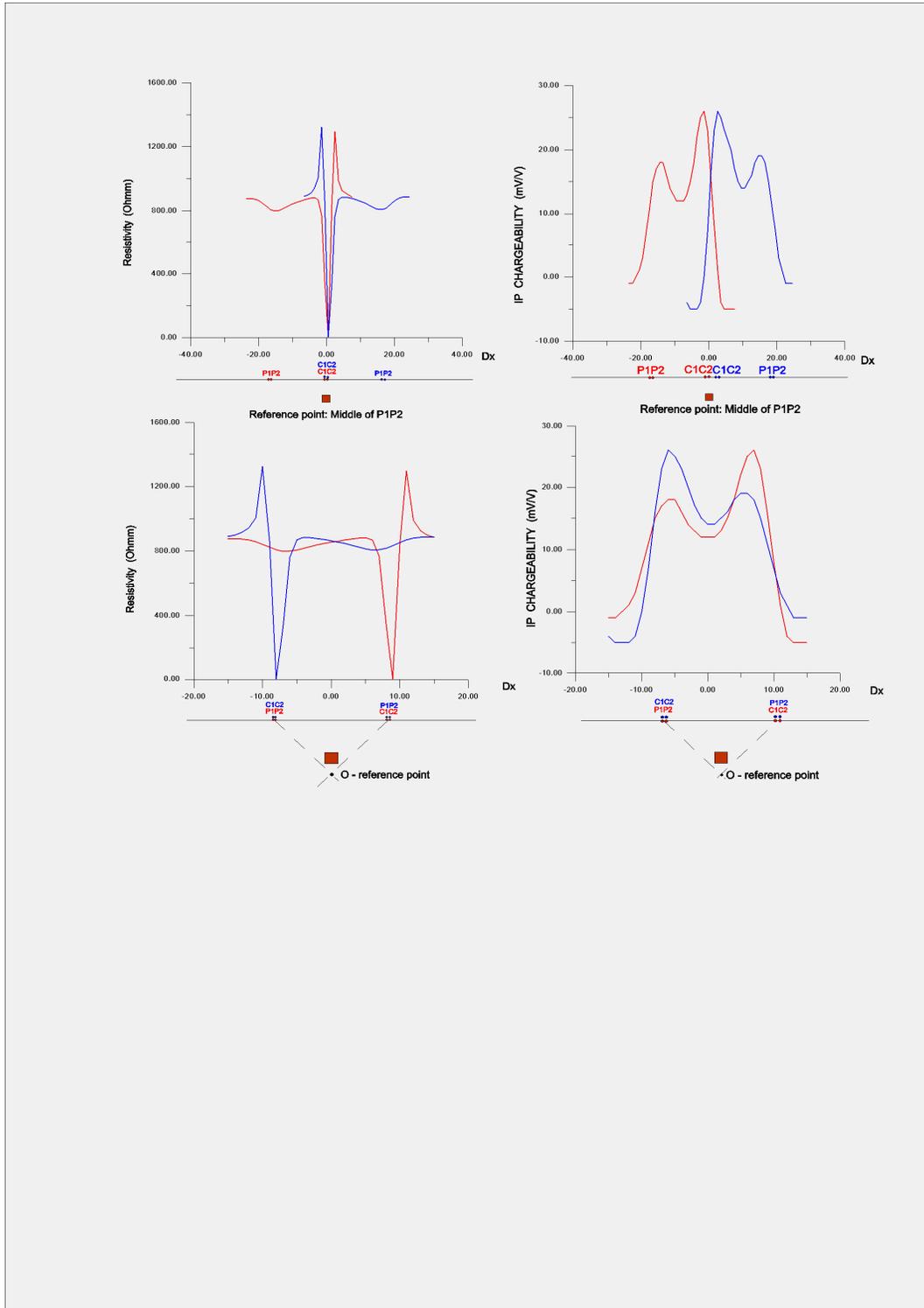


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Resistivity of the prism 1 Ohmm , IP Chargeability 500 mV/V , Resistivity of the environment 1 000 Ohmm , IP Chargeability of the environment 0.01 mV/V .

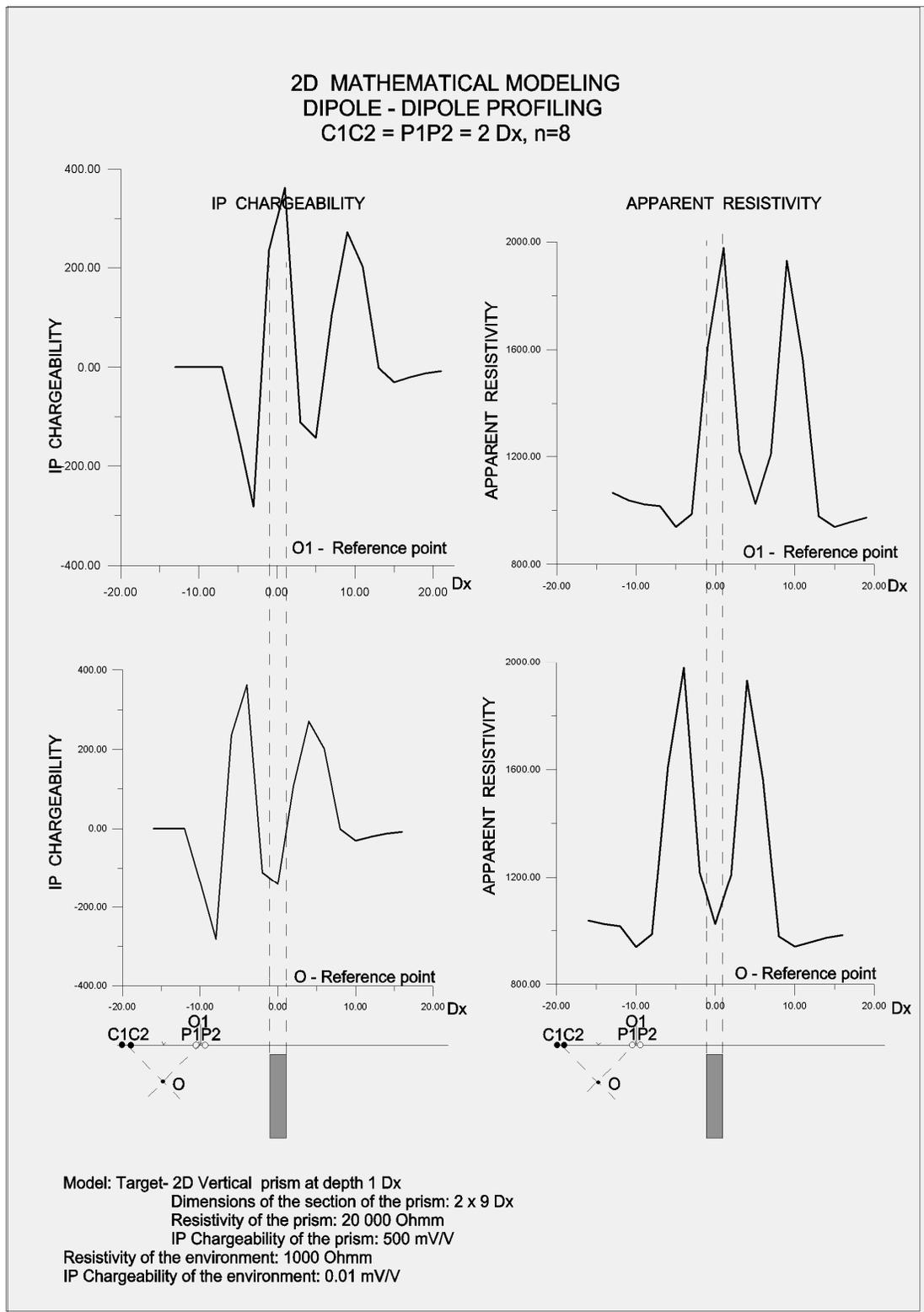


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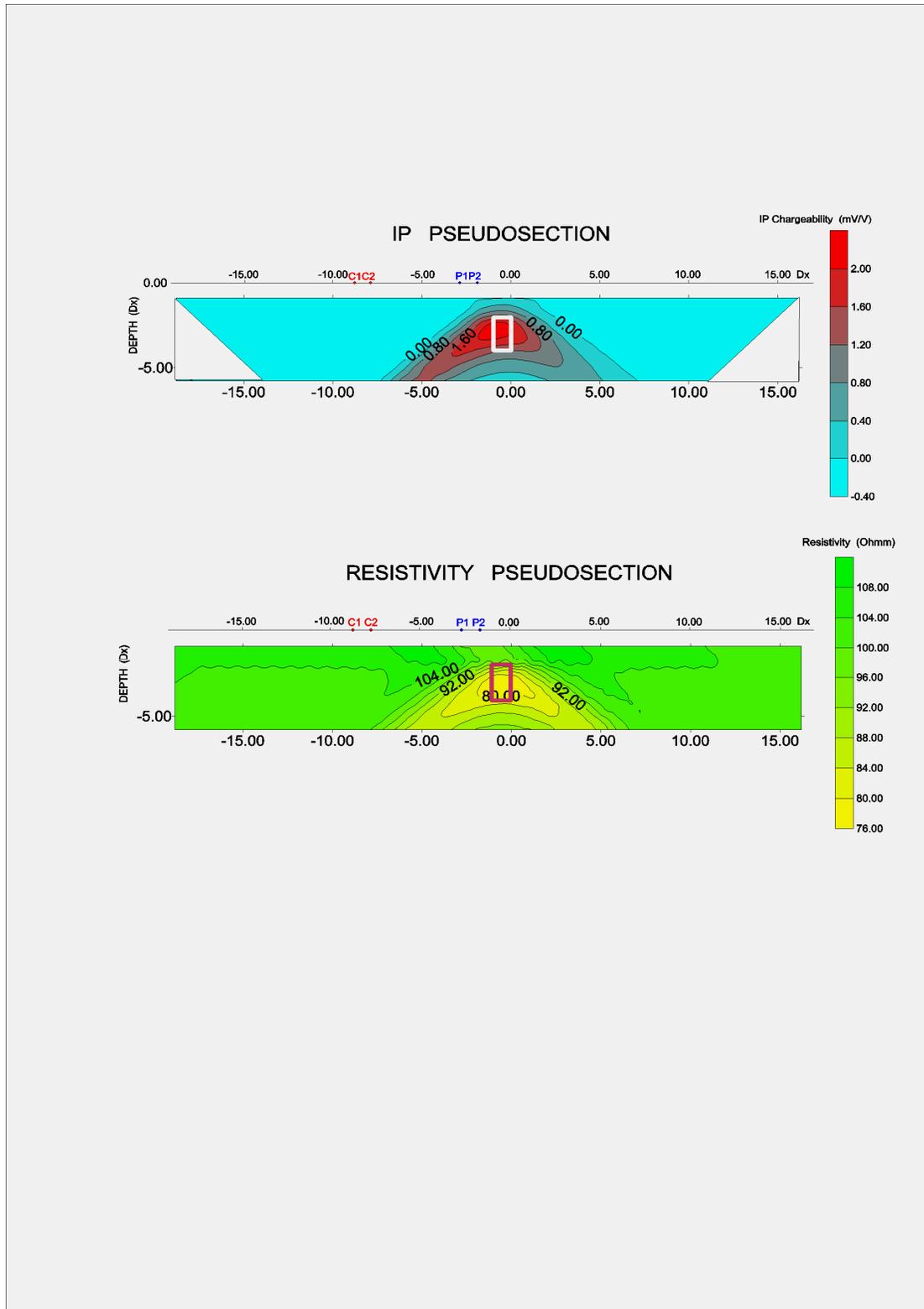


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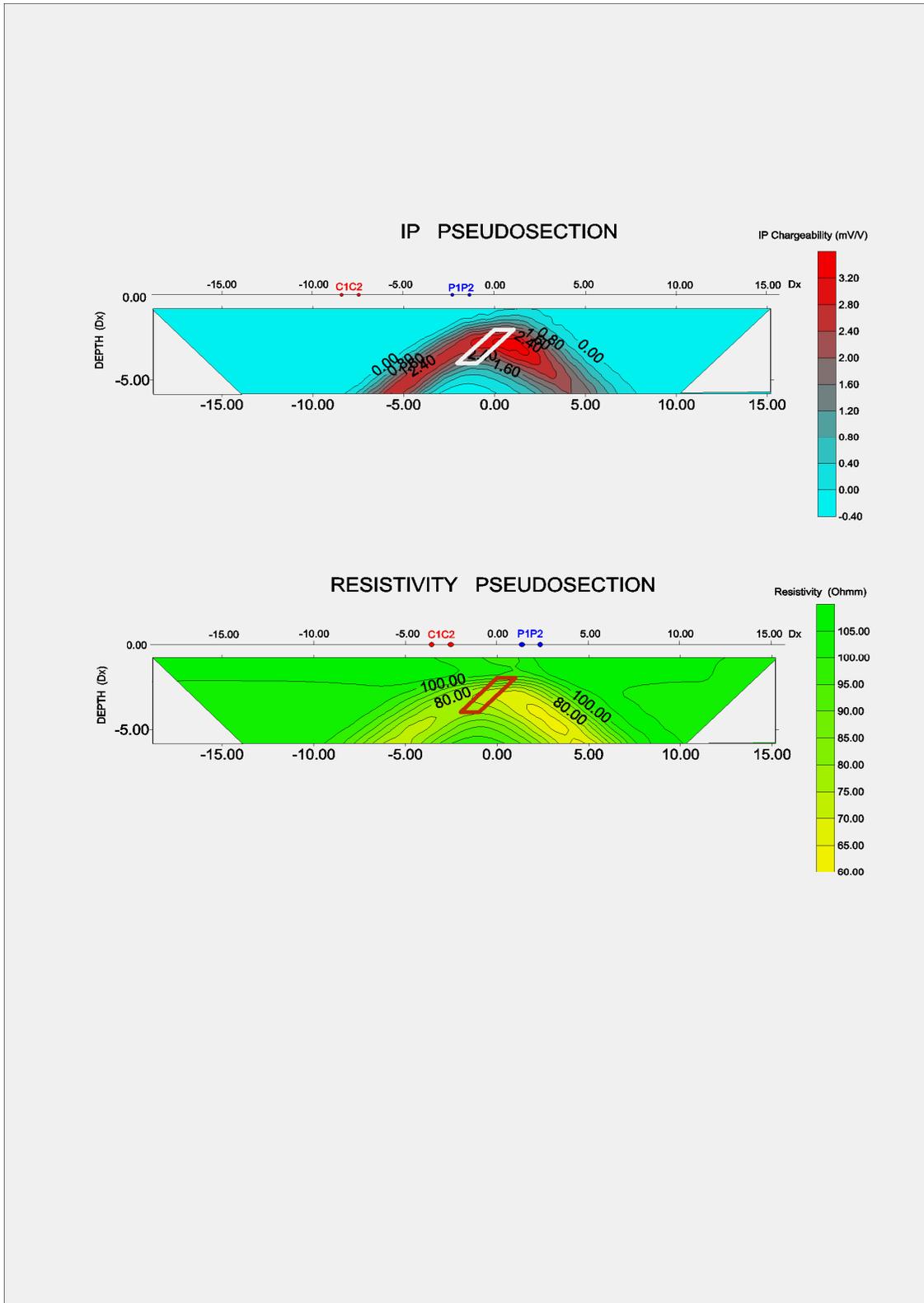


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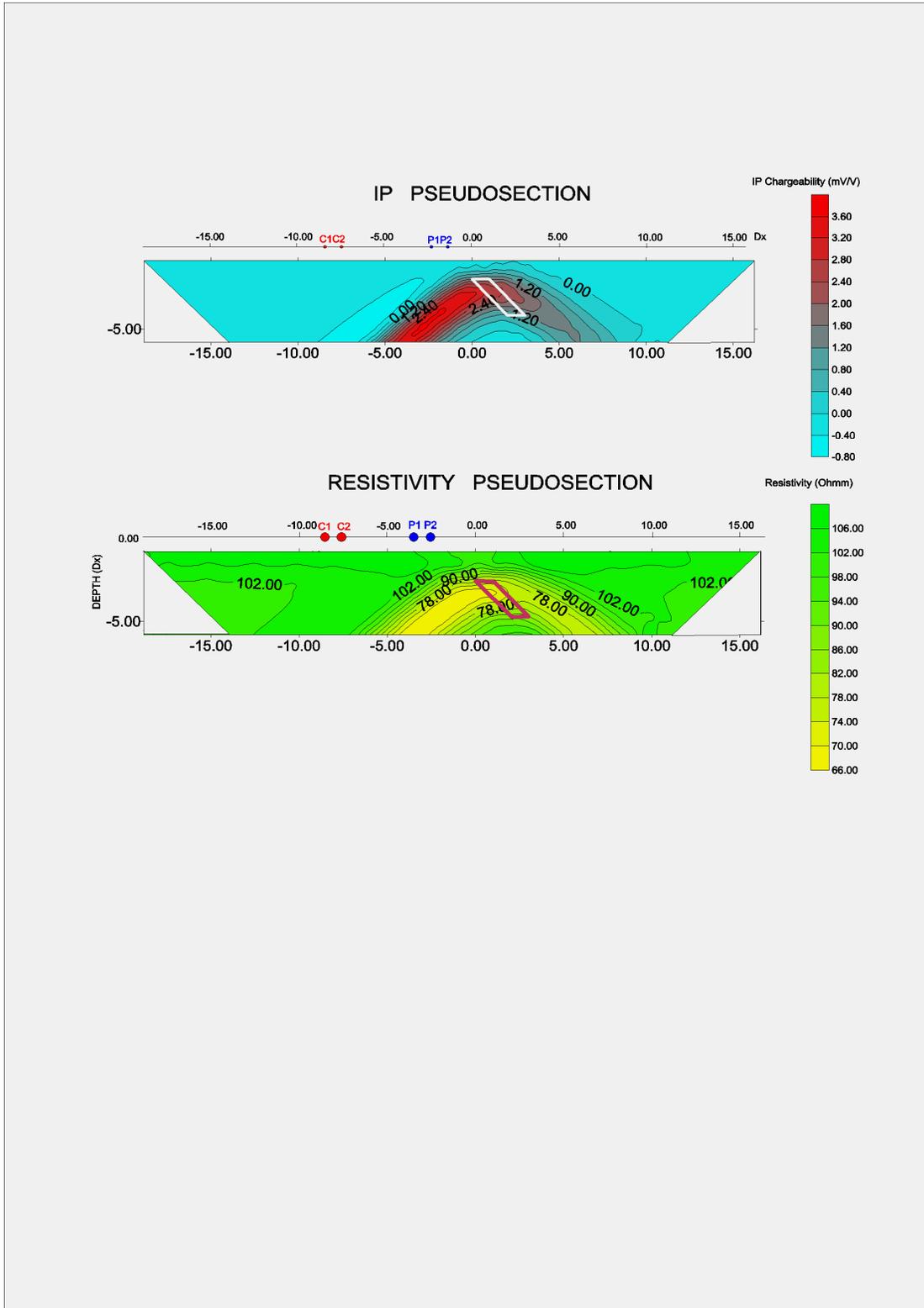


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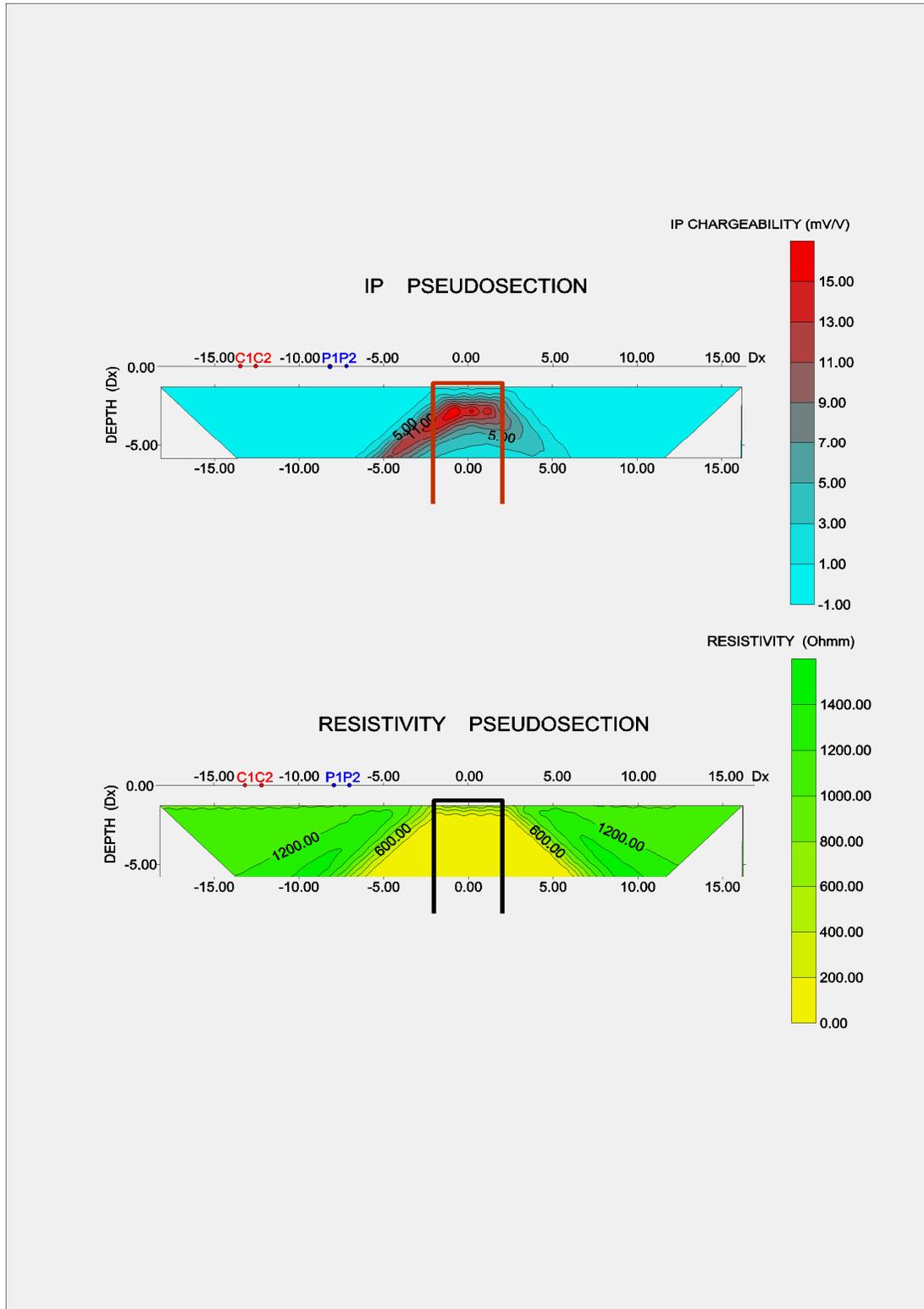
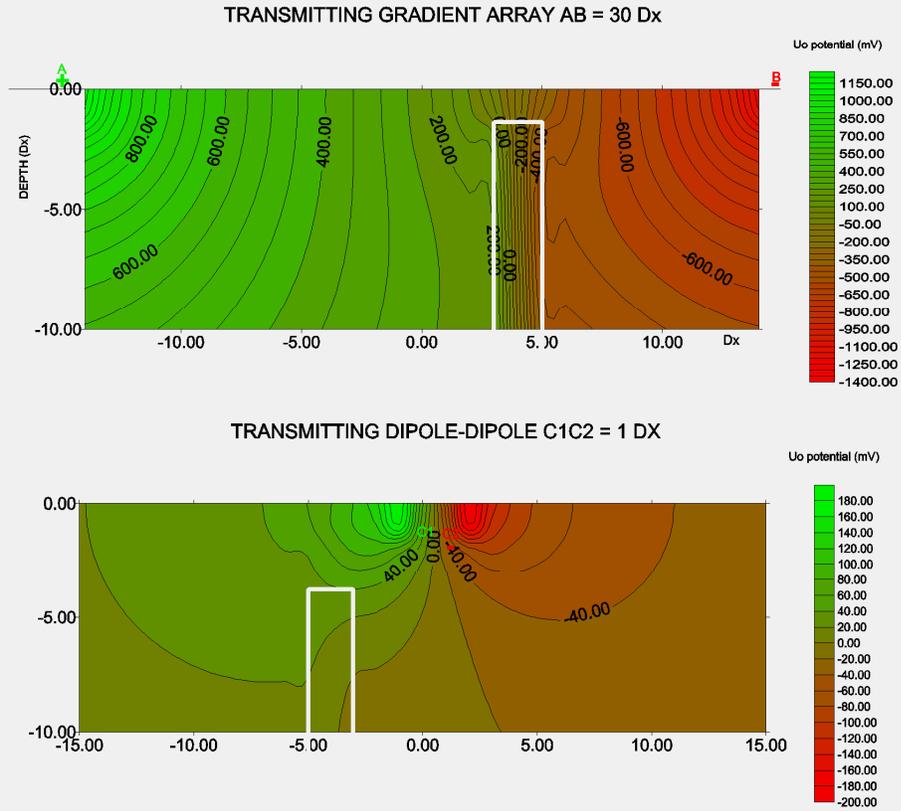


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2D RESISTIVITY MATHEMATICAL MODELING
 REAL - SECTION OF THE POTENTIAL OF POLARIZING
 ELECTRIC FIELD (U_0)



Model: Vertical dike
 Dimensions of the dike: $2 D_x \times 30 D_x \times 20 D_x$
 Resistivity of the dike: 20000 Ohmm
 Resistivity of the environment: 1000 Ohmm

Fig. 10. Realsection of the potential of polarizing electric field (U_0) of transmitting gradient array. $AB_{\max} = 30 D_x$ (a) and of transmitting dipole $C_1C_2 = 1 D_x$.

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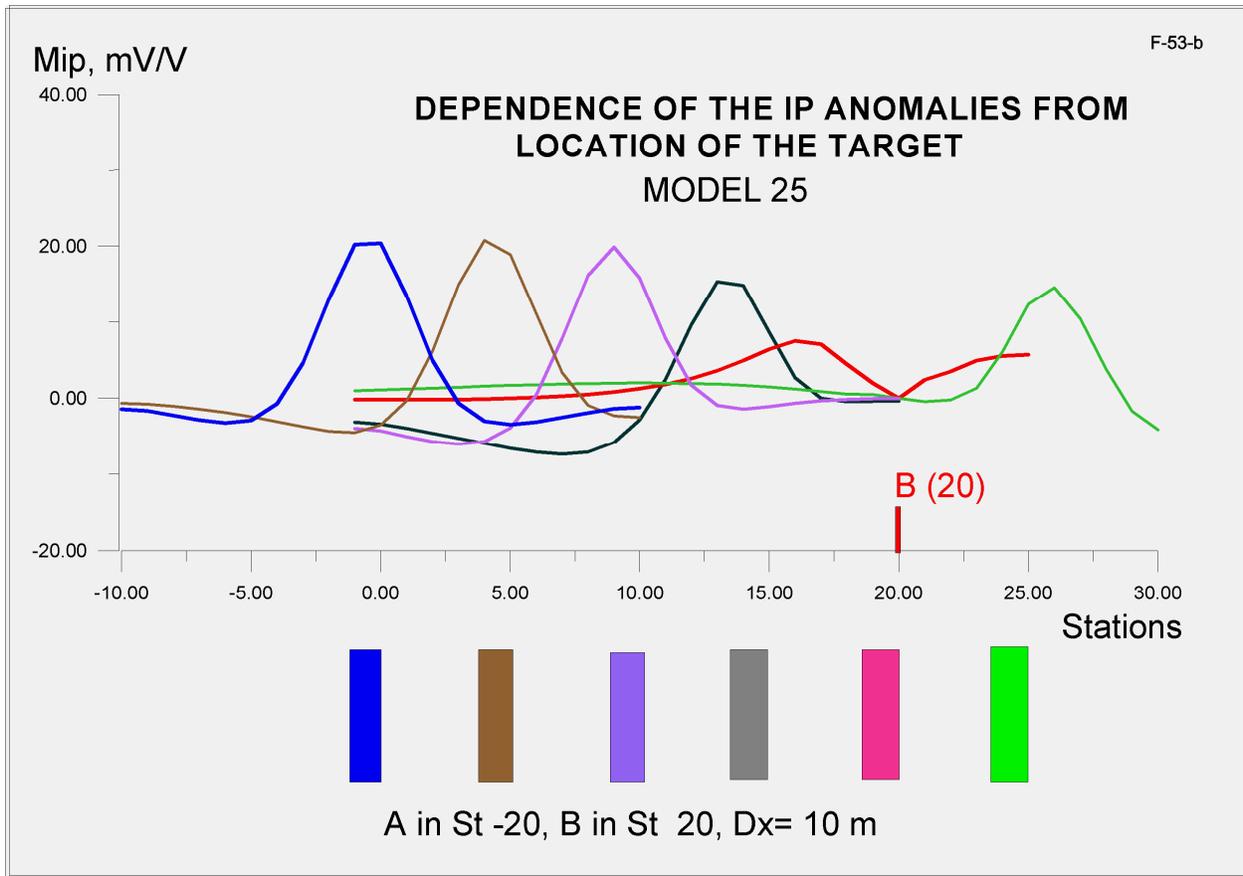


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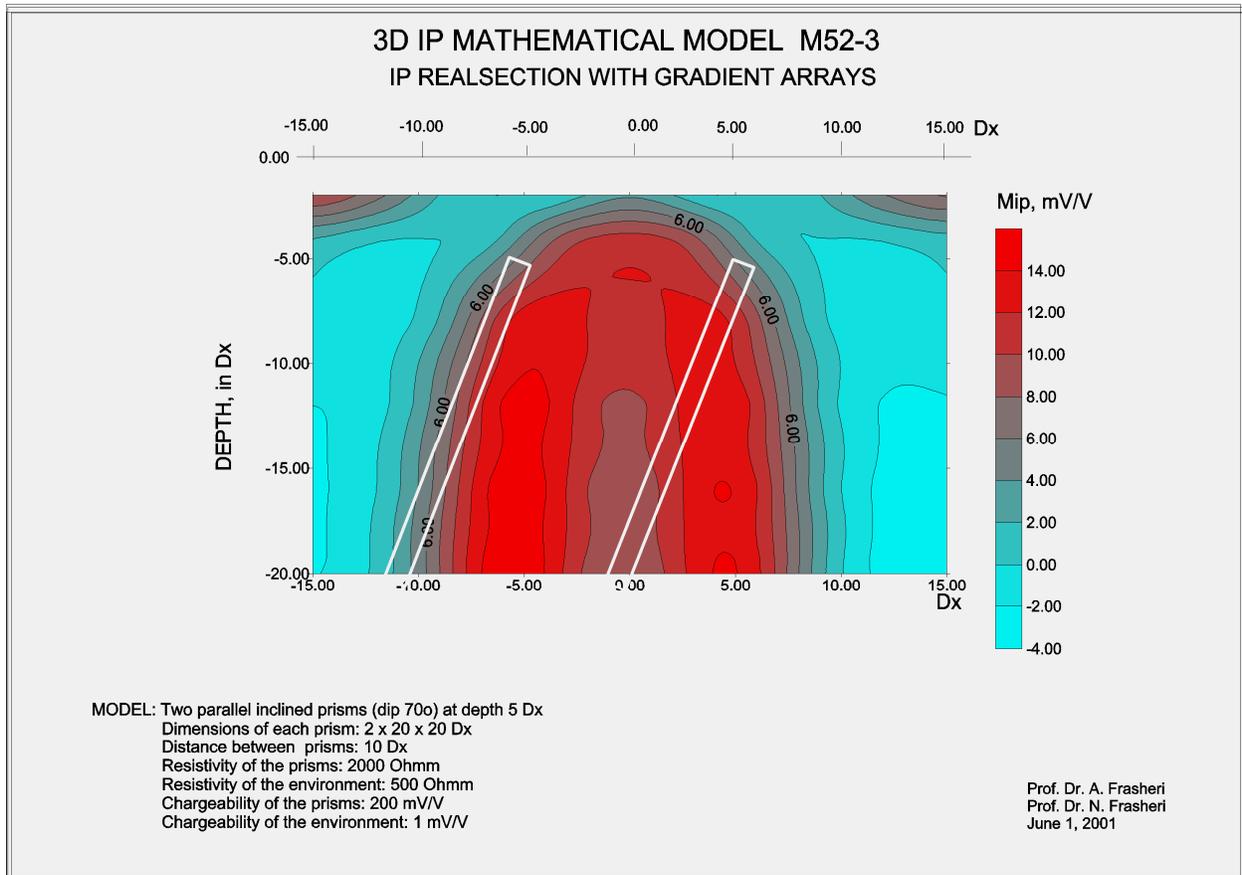


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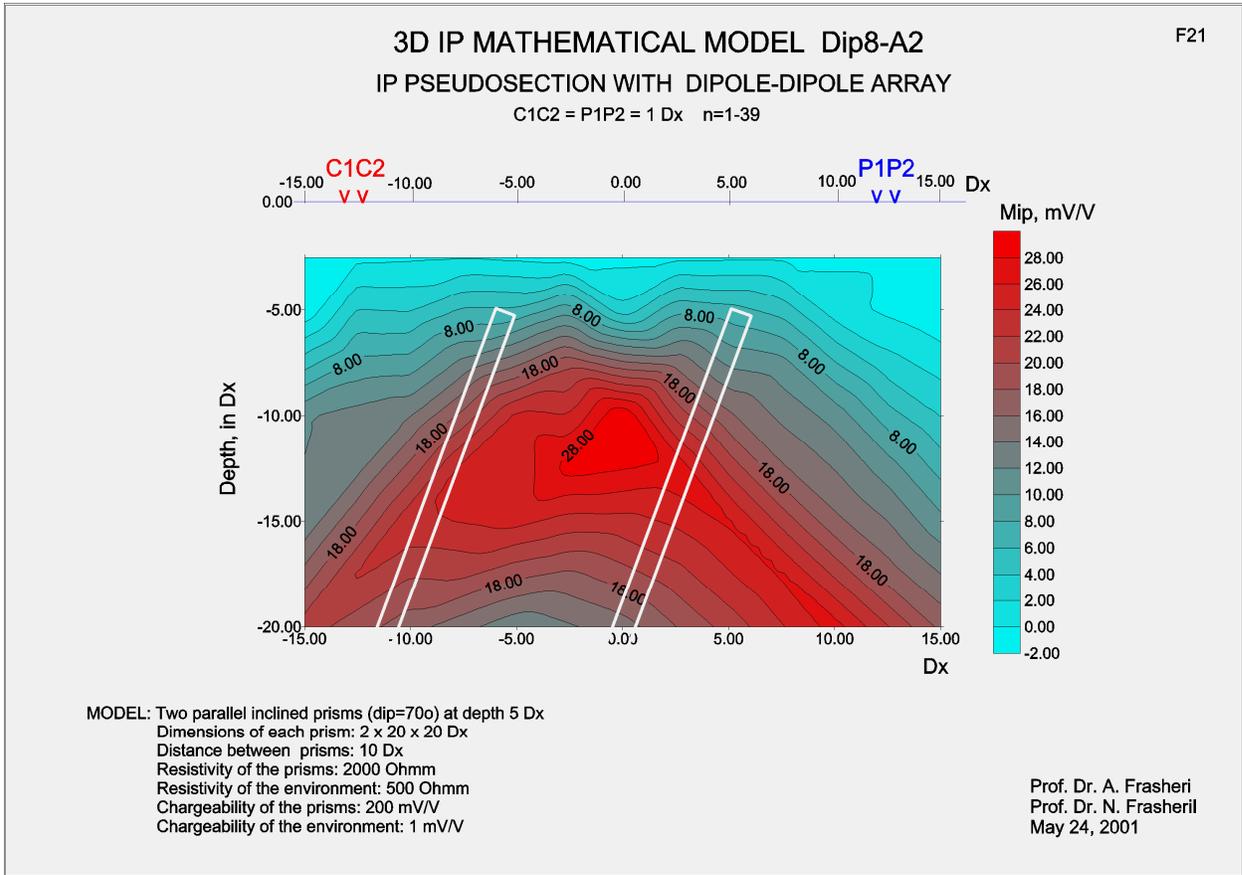


Fig. 13. IP Pseudosection with dipole-dipole array, $C_1C_2=P_1P_2=1 \text{ Dx}$, $n=1-39$.

Mathematical Model: Two parallel inclined prisms (dip=70°) at depth 5 Dx, dimensions of the prisms 1 x 20 x 20 Dx. Distance between the prisms 10 Dx, Prisms Resistivity 2 000 Ohmm, IP Chargeability 500 mV/V, Environment Resistivity 500 Ohmm , IP Chargeability 0.01 mV/V.

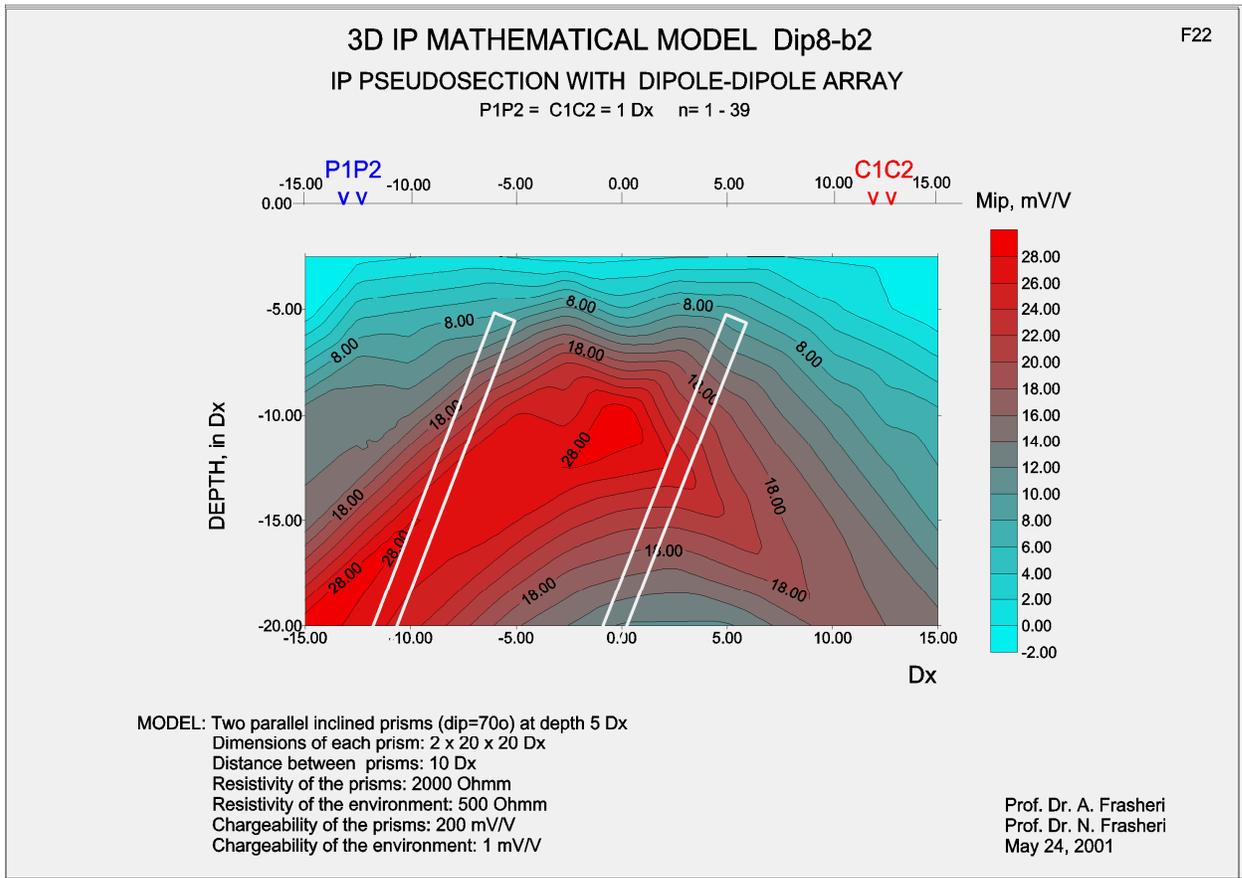


Fig. 14. IP Pseudosection with dipole-dipole array, $P_1P_2=C_1C_2=1 \text{ Dx}$, $n=1-39$.

Mathematical Model: Two parallel inclined prisms (dip=70°) at depth 5 Dx, dimensions of the prisms 1 x 20 x 20 Dx. Distance between the prisms 10 Dx, Prisms Resistivity 2 000 Ohmm, IP Chargeability 500 mV/V, Environment Resistivity 500 Ohmm , IP Chargeability 0.01 mV/V.